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Topological classification of pairs of linear mappings

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Each matrix pencil $A + \lambda B$ over a field is strictly equivalent to its *regularizing decomposition*; i.e., a direct sum $(I_r + \lambda D) \oplus (M_1 + \lambda N_1) \oplus \dots \oplus (M_t + \lambda N_t)$, in which D is a nonsingular matrix and each $M_i + \lambda N_i$ is a singular indecomposable Kronecker pencil. By [1], $A + \lambda B$ and $A' + \lambda B'$ over $\mathbb{F} = \mathbb{R}$ or \mathbb{C} are *topologically equivalent* (i.e., $A, B : \mathbb{F}^n \rightarrow \mathbb{F}^m$ and $A', B' : \mathbb{F}^n \rightarrow \mathbb{F}^m$ coincide up to homeomorphisms of \mathbb{F}^n and \mathbb{F}^m) if and only if their regularizing decompositions coincide up to permutation of summands and replacement of D by D' such that the linear operators $D, D' : \mathbb{F}^r \rightarrow \mathbb{F}^r$ coincide up to a homeomorphism of \mathbb{F}^r .

- [1] V. Futorny, T. Rybalkina, V.V. Sergeichuk, *Linear Algebra Appl.* **450**, (2014), p. 121-137.